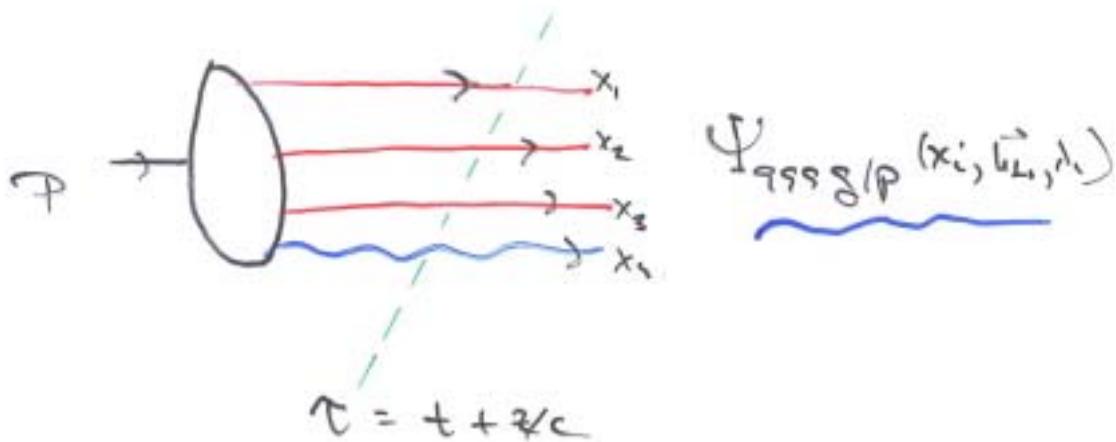


New QCD Phenomena and
QCD Light-Front Wavefunctions

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SLAC

Light-Cone 2002 LANL

August 4, 2002



$$\Psi_{q\bar{q}g/p}(x_i, \vec{k}_L, \lambda_i)$$

$$x_i = \frac{k_i^+}{p^+} = \frac{k_i^0 + k_i^\tau}{p^0 + p^\tau}, \quad \sum x_i = 1.$$

Light-Cone Wavefunctions
and QCD Phenomena

Non-Perturbative
QCD

$\{\Psi_n\}$: translation: hadrons $\Rightarrow \mathbf{q}, \mathbf{g}$

$$x_i = \frac{k_{\perp i}^+}{P^+} = \frac{k_i^0 + k_i^+}{P^0 + P^+}$$

$$\text{fixed } \tau = t + z/c \quad \text{time}$$

$$|\Psi\rangle = \sum_n |n\rangle \Psi_n(x_i, \vec{k}_{\perp i}, \lambda_i)$$

c basis

$$\sum_{i=1}^n x_i = 1, \quad \sum_{i=1}^n \vec{k}_{\perp i} = 0$$

Light-cone Fock expansion

boost invariant Frame-indep.

* Given $\{\Psi_n(x_i, \vec{k}_i, \lambda_i)\}$

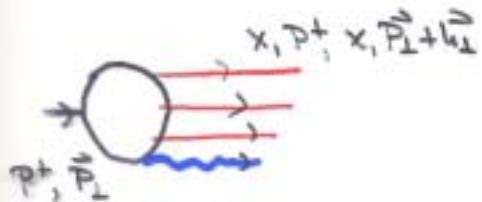
wavefunction known for all \vec{P}^{μ} !

relative coordinates

$$|\vec{P}^+, \vec{P}_{\perp}\rangle = \sum_i \Psi_n(x_i, \vec{k}_i, \lambda_i) \pi \frac{1}{\sqrt{x_i}}$$

$$|x_i \vec{P}^+, x_i \vec{P}_{\perp} + \vec{k}_i, \lambda_i\rangle$$

absolute coordinates



In equal-time theory (instant form)

boost's mix with interactions

changing $\vec{P} \rightarrow \vec{P}'$ as complicated

as solving $H|\Psi\rangle = E|\Psi\rangle$

L.C. wfs - $\left\{ \begin{array}{l} \text{rest frame} \\ \vec{P} + \vec{0} \\ \text{frame-independent!} \end{array} \right.$

$$\tau = t + \frac{z}{c}$$

Dirac
Bjorken, Drell, Sypek
Lepage + DDG
Pauli + DDG

Equation of motion

$$i \frac{\partial}{\partial \tau} |\Psi_n\rangle = \hat{P}^- |\Psi_n\rangle = \frac{m_n^2 + \vec{P}_\perp^2}{\hat{P}^+} |\Psi_n\rangle$$

$$H_{LC} = \hat{P}^- \hat{P}^+ - \hat{P}_\perp^2$$

\hat{P}^+, \hat{P}_\perp
kinematical

$$H_{LC} |\Psi_n\rangle = m_n^2 |\Psi_n\rangle$$

⇒ eigenvalue problem for LC Hamiltonian

Insert complete set of H_{LC}^0 eigenstates
 $\sum_n |n\rangle \langle n| = I$

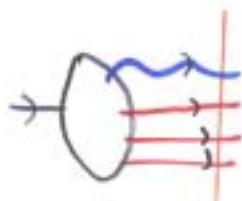
$$\sum_n \langle m | H_{LC} | n \rangle \langle n | \Psi_n \rangle = m_n^2 \langle m | \Psi_n \rangle$$

⇒ Heisenberg matrix form of eigenvalue problem

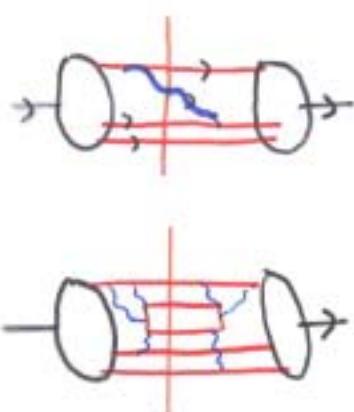
$$|\Psi_n\rangle = \sum_n |n\rangle \langle n | \Psi_n \rangle = \sum_n |n\rangle \Psi_n^{(x_1, k_1, \dots)}$$

⇒ LC Fock expansion of eigenstate $|\Psi_n\rangle$

Hadrons: complex relativistic systems

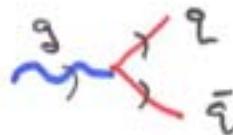


fluctuations in particle no.,
size, spin, color



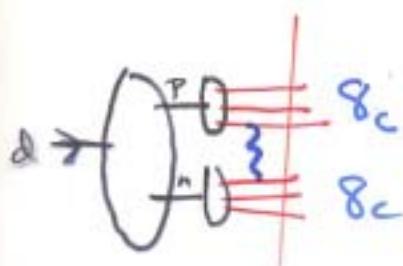
gluons intrinsic to hadron structure

$\left\{ \begin{array}{l} \bar{u}(x) \neq \bar{d}(x) \Rightarrow \text{correlation} \\ \bar{s}(x) \neq \bar{\bar{s}}(x) ? \end{array} \right.$
 ∴ Sea not from gluon splitting $\stackrel{\text{prob}}{\rightarrow}$



$$q(x) = \bar{q}(x_0)$$

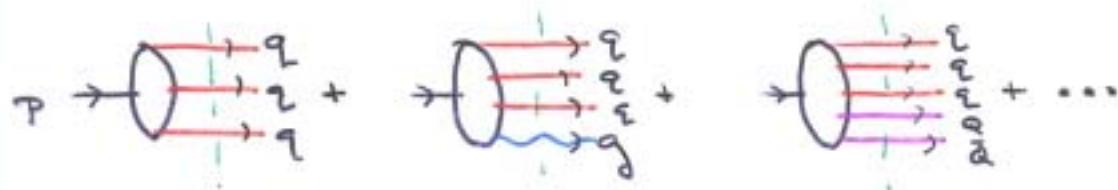
$$\bar{q}(x) = \bar{\bar{q}}(x_0)$$



"Hidden color" in nuclei

$$\Psi_d \neq \Psi_n \otimes \Psi_p$$

Light-Cone Fock Representation of Hadrons



$$|P\rangle = \sum_n |n\rangle \Psi_n(x_i, \vec{k}_{xi}, \lambda_i)$$

$\approx \sum x_i = 1, \sum \vec{k}_{xi} = 0$

► Explicit solutions QCD(1+1), "collinear" QCD
using "DLCQ"
SGB, Pauk, Herbstschl
Antonuccio, Dalley

► Calculate structure functions modulo FSI

$$q(x), g(x), Q(x)$$

spin-dependence

► Calculate Regge behaviour $x \rightarrow 0$, BFKL
using "ladder relations" spin-dependence
Mueller, SIB, Antonuccio, Dalley

► $x \rightarrow 1$ constraints Lepage, SITZ, Burkhardt, Schub

► Properties of heavy quark sea $s(x) \neq \bar{s}(x)$
extrinsic vs intrinsic Kogut Ma
physics of $\Delta \Sigma$, anomaly Schmidt
Ball SGB
Schwinger

Light-Cone Wavefunctions

encode all helicity, transversity
distributions

$$q_{\lambda/\lambda_p} = \int \left| \begin{array}{c} \rightarrow \\ \lambda_p \end{array} \right| \left| \begin{array}{c} x, \lambda \\ \rightarrow \\ \rightarrow \\ \rightarrow \end{array} \right|^2$$

$$q_{\lambda/\lambda_p}(x, \Lambda) \quad \left\{ \begin{array}{l} \text{transversity: density matrix} \\ \text{light-cone helicity} \end{array} \right.$$

$$= \sum_{n,q} \int \left| \psi_{n,\lambda_p}^{(\Lambda)} (x_i, \vec{k}_{2i}, \lambda_i) \right|^2 \prod_{i=1}^n dx_i \prod_{j=1}^m d^2 k_{2j}$$

$$\delta(\sum_i x_i - 1) \delta(\sum_i \vec{k}_{2i})$$

$$\delta(x - x_q) \delta_{\lambda, \lambda_q}$$

$$\Theta(\Lambda^2 - m_i^2)$$

Factorization
Light-cone Scheme

(a) Light Cone Fock Expansion

$$|p\rangle = \sum_{\Psi_{uud}} \psi_{uud} |uud\rangle + \sum_{\Psi_{uudg}} \psi_{uudg} |uudg\rangle + \dots$$

$$\langle p | qqq \rangle : \sum_{\Psi_{uud}} \psi_{uud} |x_1, \vec{k}_{\perp 1}, \lambda_1 \rangle + |x_2, \vec{k}_{\perp 2}, \lambda_2 \rangle + |x_3, \vec{k}_{\perp 3}, \lambda_3 \rangle$$

$$\psi_n(x_i, \vec{k}_{\perp i}, \lambda_i) : \sum_{i=1}^n x_i = 1, \sum_{i=1}^n \vec{k}_{\perp i} = 0$$

(b) Distribution Amplitude

$$\phi_M^{(x, Q)} = \int d^2 k_{\perp} \rightarrow \sum_{\Psi_2} \psi_2(x, \vec{k}_{\perp}) + (1-x, -\vec{k}_{\perp})$$

$$M_n^2 < Q^2$$

(c) Deep Inelastic $\ell p \rightarrow \ell' X \langle p | J^+(z) J^+(0) | p \rangle$

$$\gamma^* q \rightarrow q \gamma^* = \sum_n \sum_{\Psi_n} \psi_n(x, \vec{k}_{\perp}) \gamma^* q \rightarrow q \gamma^*$$

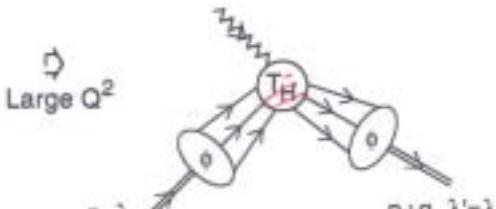
$$q(x_{B_J}, Q) = \sum_n \int \prod d^2 k_{\perp} dx \left| \sum_{\Psi_n} \psi_n(x, \vec{k}_{\perp}) \right|^2$$

$$M_n^2 < Q^2, x_q = x_{B_J}$$

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(d) Form Factors $\ell p \rightarrow \ell' p' \langle p' | \lambda' | J^+(0) | p \lambda \rangle$

$$F_{\lambda \lambda'}(Q^2) = \sum_n x_i \vec{k}_{\perp i} \rightarrow \sum_{\Psi_n} \psi_n(p, \lambda) \rightarrow \sum_{\Psi_n} \psi_n(p+q, \lambda')$$



$$T_H = \sum x_1 \rightarrow y_1 + x_2 \rightarrow y_2 + \dots$$

$$= \frac{\alpha_s^2}{Q^4} f(x_i, y_i)$$

(e) Compton $\gamma p \rightarrow \gamma' p' \langle p' | J^\mu(z) J^\nu(0) | p \rangle$

Large s, t

$$\gamma p \rightarrow \gamma' p' = \sum_{\Psi_n} \psi_n(p, \lambda) \gamma p \rightarrow \gamma' p'$$

$$p, \lambda \rightarrow p+q, \lambda' = \lambda$$

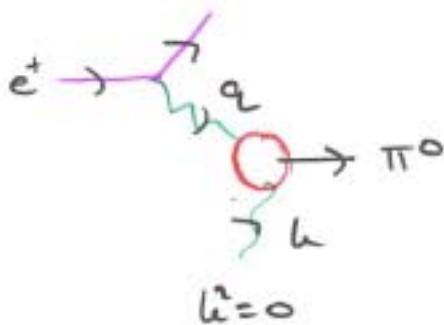
$$\gamma k \rightarrow k' = \sum_{\Psi_n} \psi_n(p, \lambda) \gamma k \rightarrow k'$$

$$T_H^{\text{Compton}} = \sum x_1 \rightarrow y_1 + x_2 \rightarrow y_2 + \dots$$

$$= \frac{\alpha_s^2}{P_T^4} f(x_i, y_i, \theta_{cm})$$

$$\gamma^* \gamma \rightarrow \pi^0, n, n', n_c \dots$$

Simplest example of exclusive process

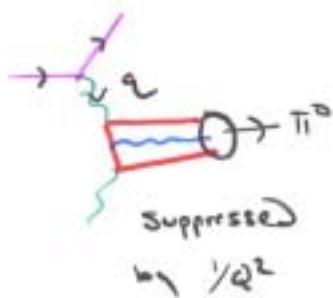
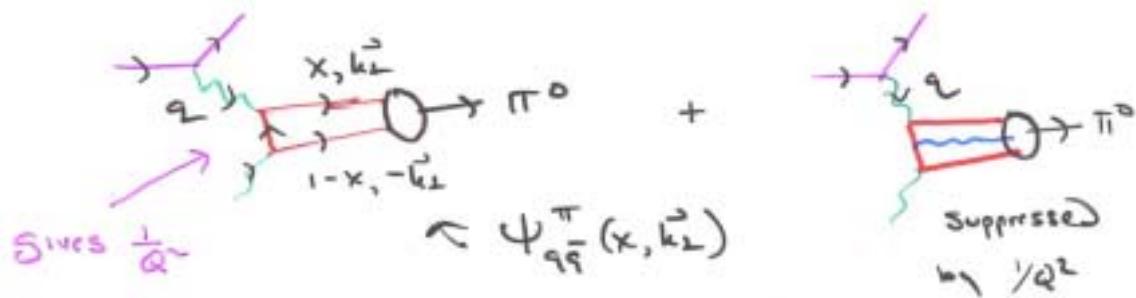


$$F_{\gamma\pi^0}(q^2)$$

$$\pi^0 \rightarrow \gamma\gamma \text{ at } q^2 = 0.$$

For $Q^2 \gg \Lambda_{QCD}^2$ analyse in PQCD

Large
SJS

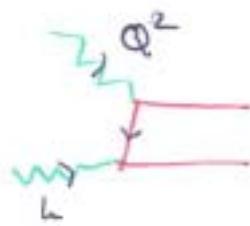
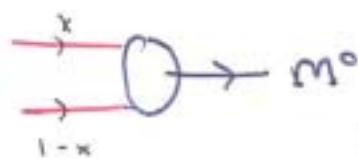


$$* F_{\gamma\pi^0}(Q^2) = \frac{1}{Q^2} 2\sqrt{n_e} (e_u^2 - e_d^2) \int_0^1 dx \left(\frac{1}{x} + \frac{1}{1-x} \right) \phi_\pi(x, Q)$$

$$* \phi_\pi(x, Q) = \int_0^{\infty} \frac{d^2 k_\perp}{16\pi^3} \Psi_{q\bar{q}}^\pi(x, \vec{k}_\perp)$$

pion distribution amplitude

PQCD : $F_{\gamma \rightarrow M^0}(Q^2) \sim \frac{1}{Q^2} \int_0^1 \frac{dx}{1-x} \phi_m(x, Q)$

 T_H  $b_L^2 < Q^2$

$$\phi_m(x, Q) = \int d^2 b_L \psi_{q\bar{q}}(x, b_L)$$

- * $T_H (\gamma^* \gamma \rightarrow q\bar{q}) \sim \frac{1}{Q^2(1-x)}$
 $\Theta(Q)$ ^{collinear}

- * Higher Fock states : $\frac{1}{Q^4}$ no

Other diagrams $\Theta(\alpha_s(Q^2))!$

- * $\phi_m(x, Q) = \sum_{n=0}^{\infty} a_n P_n(x) \left(\ln \frac{Q^2}{\Lambda^2}\right)^{-\gamma_n}$ BBJ
 $\log \text{evolution}$

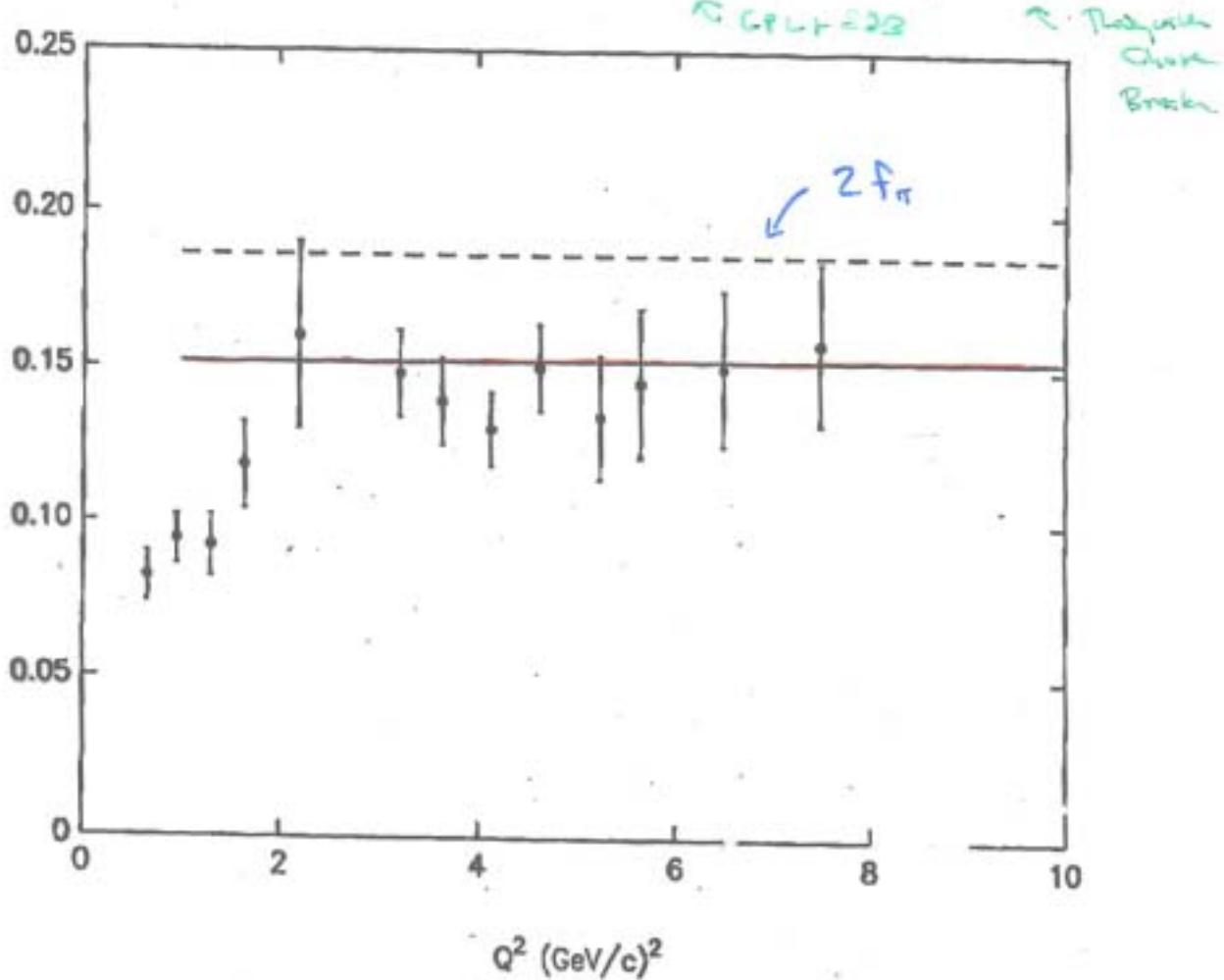
- * $\lambda_m = \lambda_q + \lambda_{\bar{q}} = 0.$ HHC \int_0^1

** Small part of Fock state dominates

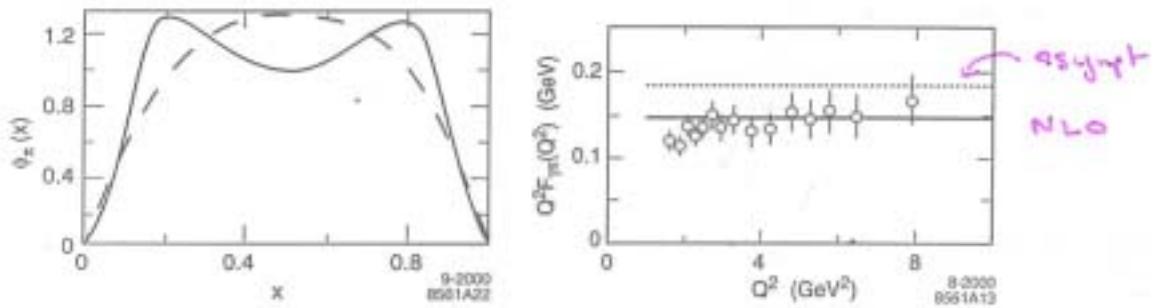
$$\phi_m \sim \psi(x, b_L \sim \frac{1}{Q})$$

$$\phi = \phi_{\text{eq}, p_T} \\ = \sqrt{x} \times (1-x) f_\pi$$

$$Q^2 F_{\pi\gamma}(Q^2) = 2f_\pi \left[1 - \frac{\pi}{3\pi} \alpha_V(e^{-3Q^2}) \right]$$



CLEO (Sevinov et al)

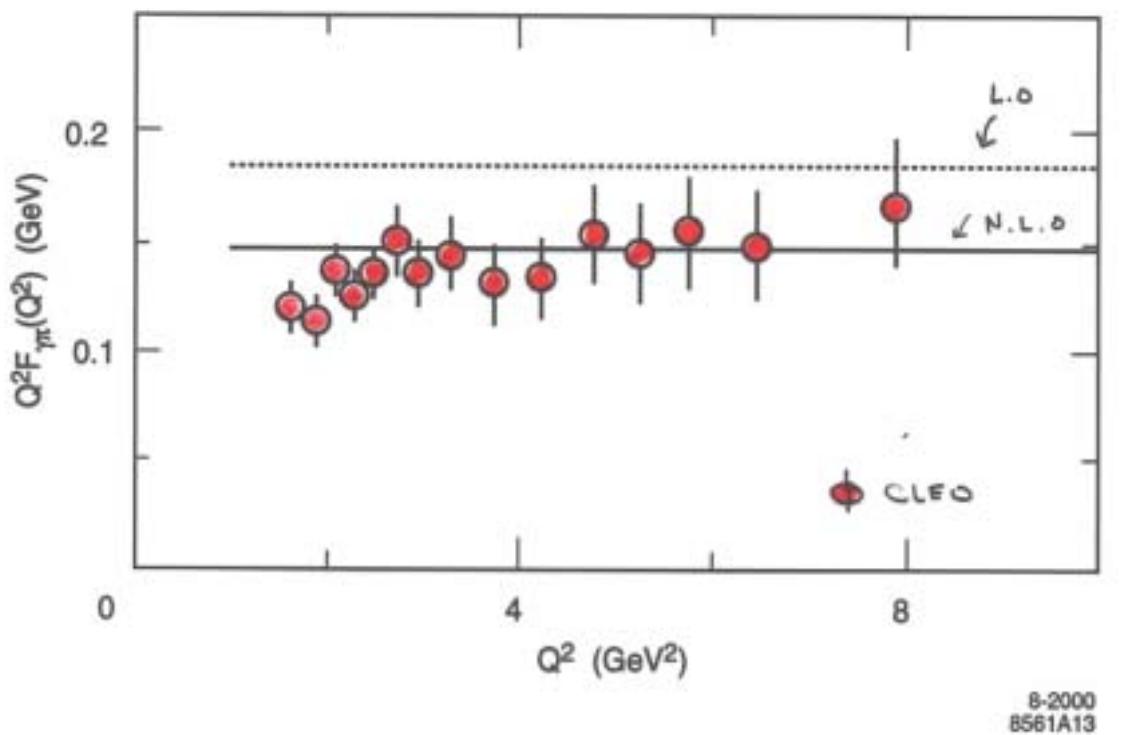


— transverse lattice/DLCQ

Delaney

--- Asymptotic dist. ampl.

Burkhardt



assumes $\phi_{\pi\pi}(x) = \phi_{\pi\pi}^{asymp}(x)$

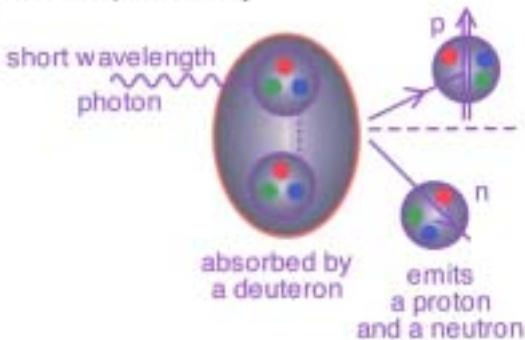
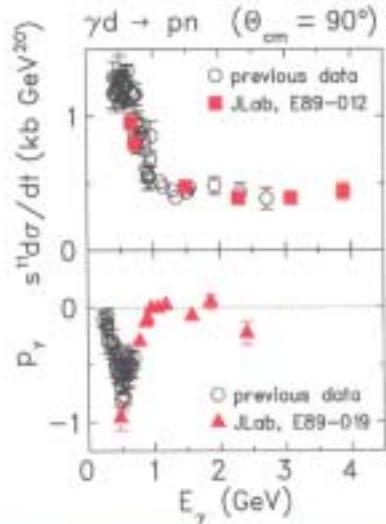
$= \sqrt{3} f_\pi \times (1-x)$



SHORT-DISTANCE STRUCTURE of the DEUTERON

Jefferson Lab (E89 - 012, E89 - 019)

Do we see the effects of
quarks and gluons in a
nuclear reaction ?



- Reaction probability is consistent with quark counting rules at high photon energy.
- Polarization vanishes at same photon energy that reaction probability begins scaling.
- First glimpse of the transition region.



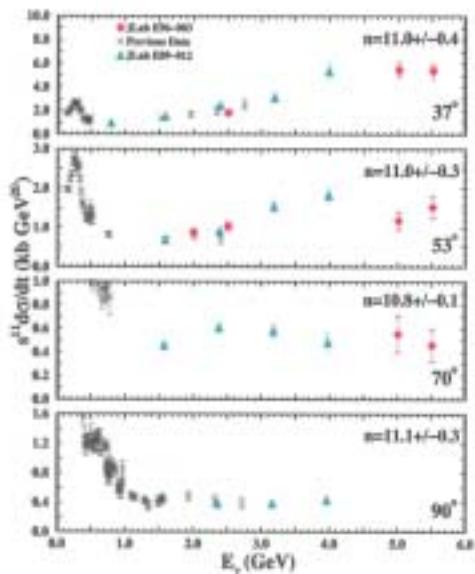
High Energy Photodisintegration of the Deuteron

Jefferson Lab (E96 - 003)

Is there a threshold for scaling for the $\gamma d \rightarrow pn$ reaction?

Quark counting rules $\Rightarrow \frac{d\sigma}{dt} \sim \frac{1}{s^{11}}$

- Evidence for scaling observed for the first time at forward angles ($\theta_{c.m.} = 37^\circ, 53^\circ$).
- A scaling threshold in transverse momentum of $P_T = 1.3 \pm 0.1$ GeV/c is consistent with all existing data.



E.C. Schulte et al., Phys. Rev. Lett. 87, 102302 (2001)

Christie, White, Ji, Sato
Lemire.

✓ New results for $e\bar{p}_T \rightarrow e\bar{p}_T$ from JLAB

$$\frac{G_E(t)}{G_M(t)} \underset{\text{decreasing}}{\sim} \Rightarrow \sqrt{-t} \frac{F_2(t)}{F_1(t)} \underset{\sim}{\sim} \text{const}$$

Need higher t , timelike $\bar{p}\bar{p} \rightarrow l\bar{l}$, $l\bar{l} \rightarrow pp^-$
done!



$$\frac{d\sigma}{ds} \propto |G_M(s)|^2 (1 + \cos^2 \theta_{cm}) + \frac{4\pi^2}{s} |G_E(s)|^2 \sin^2 \theta$$

SSA

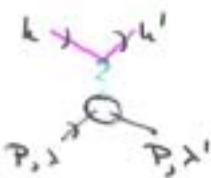
$$P_y = \frac{-\sin 2\theta_{cm} \operatorname{Im} G_E^* G_M \frac{2M}{\sqrt{s}}}{|G_M|^2 (1 + \cos^2 \theta) + \frac{4\pi^2}{s} |G_E|^2 \sin^2 \theta}$$

Pol transp.

$$P_x = P_\ell \frac{2 \sin \theta_{cm} \operatorname{Re} G_E^* G_M \frac{2M}{\sqrt{s}}}{|G_M|^2 (1 + \cos^2 \theta) + \frac{4\pi^2}{s} |G_E|^2 \sin^2 \theta}$$

does G_E change sign?

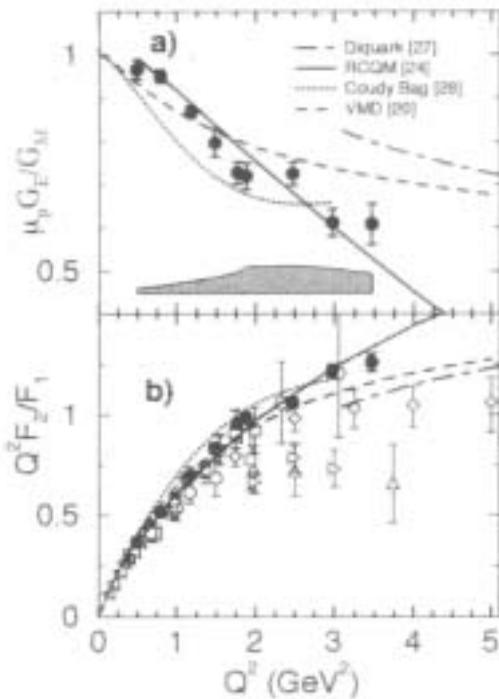
does $\frac{d\sigma}{ds} \sim (1 + \cos^2 \theta)$ PQCD HMC.



JLab uses polarization transfer
to recoil proton

$$\ell^+ \langle p', x' | j_\mu | p, x \rangle \propto G_E, G_M$$

$$\frac{P_x}{P_y} = \frac{G_E}{G_M} \frac{z_h}{(kT)^2 f_{\text{rec}}}$$



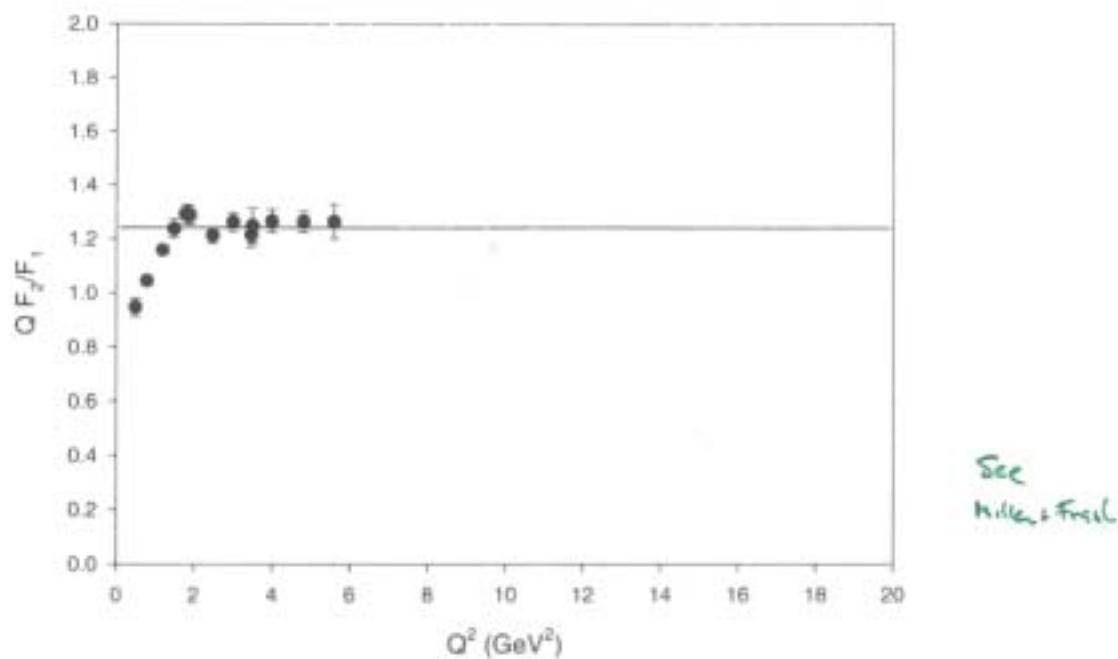
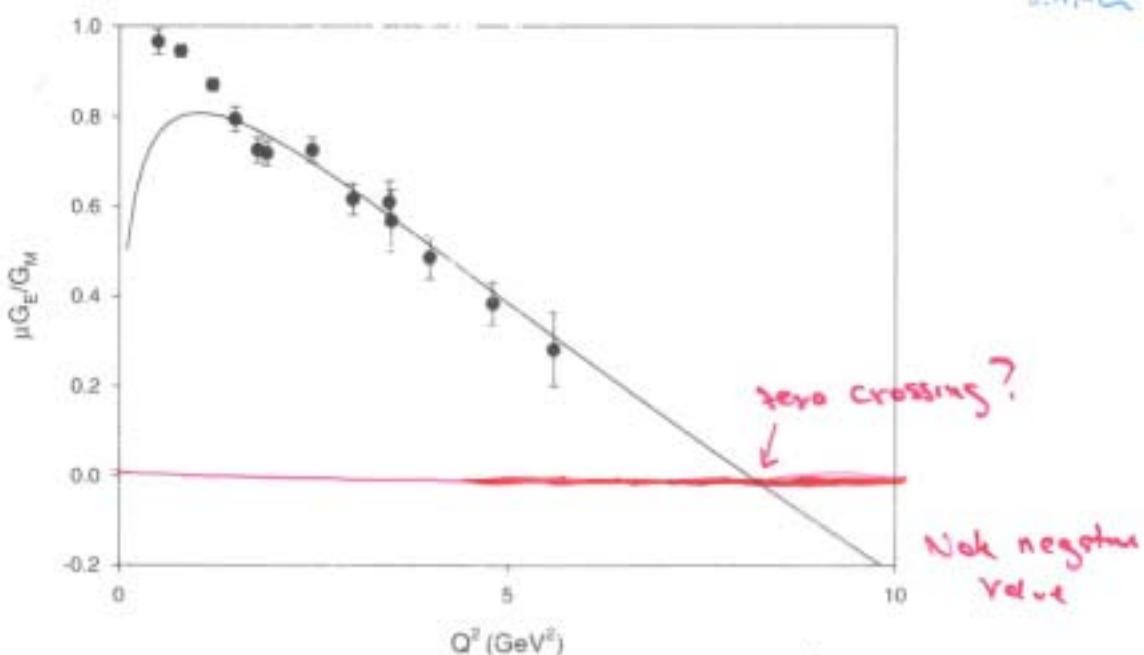
\rightarrow Jefferson
Lab

$$p_{QCD} \quad \frac{F_2}{F_1} \sim \frac{1}{Q^2} \quad \text{diquark model?}$$

$$F_2/F_1 = 0.66/\sqrt{t}$$

$$\tau_0 = 0.7 \text{ fm}^{-1}$$

$\mu^2 \text{ MeV}$



J. Hiller
D.S. Hwang
SJR

[PQCD - motivated fit to JLab data]

$$\frac{F_2(Q^2)}{F_1(Q^2)} = \frac{M_A}{1 + \frac{Q^2}{0.96 \text{ GeV}^2} \log^b \left(1 + \frac{Q^2}{4m_\pi^2} \right)}$$

$$M_A = 1.79$$

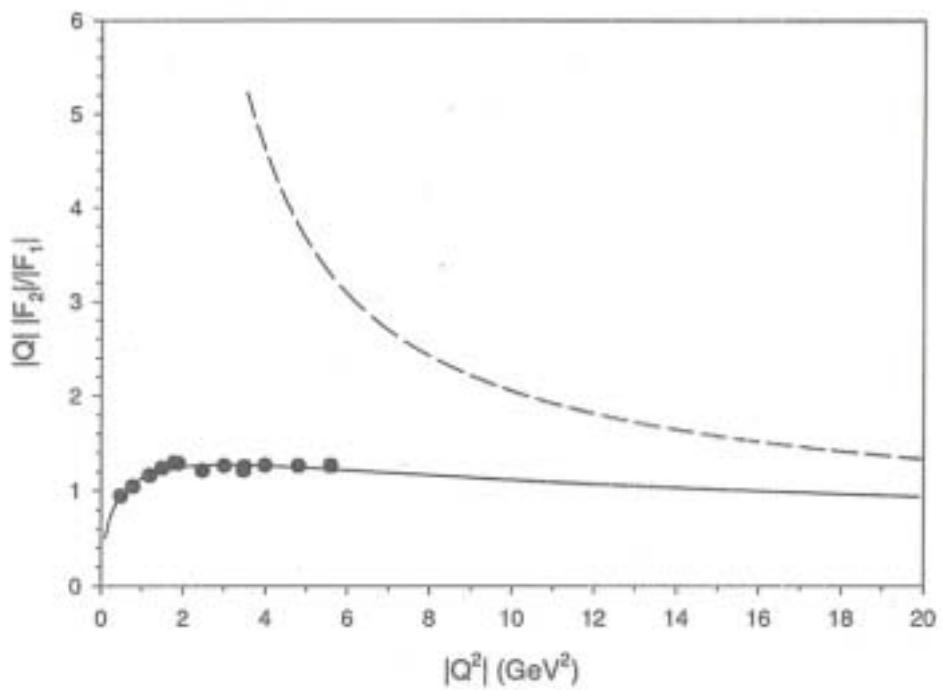
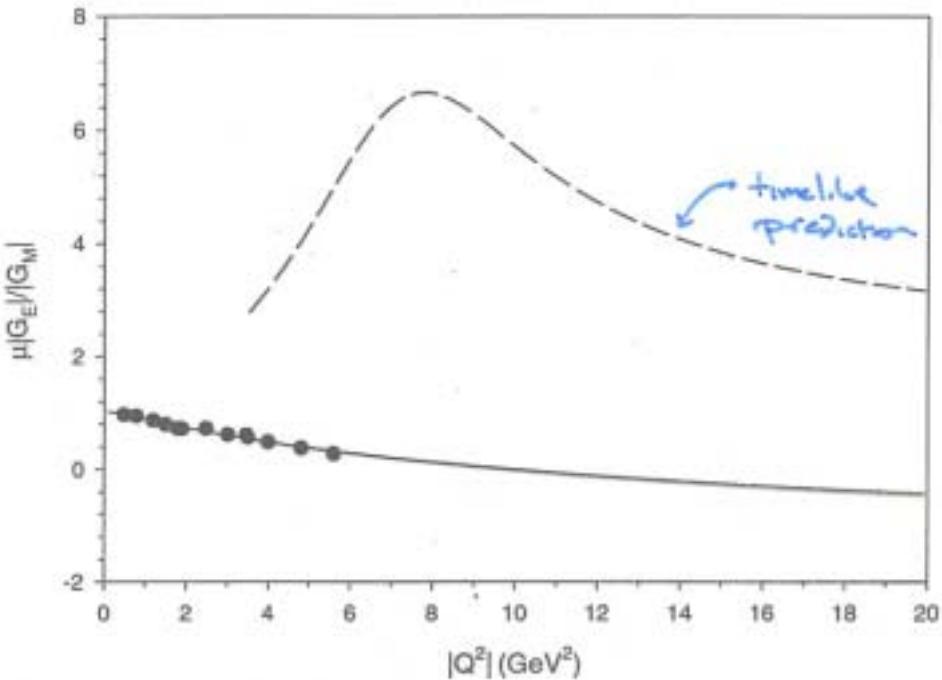
$$Q^2 = -q^2 = -t$$

$$b = -0.6$$

$$\Rightarrow \frac{Q^2 F_2(Q^2)}{F_1(Q^2)} \sim \log^{-b} Q^2 \quad Q^2 \rightarrow \infty$$

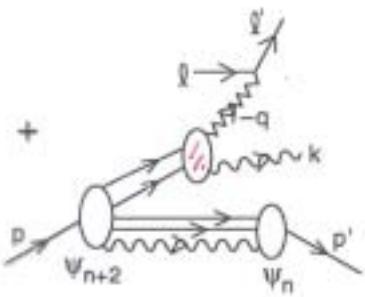
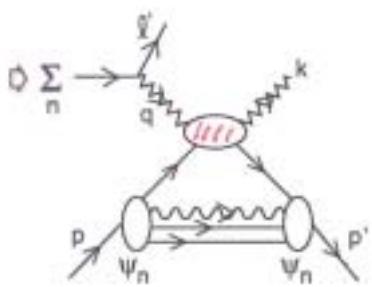
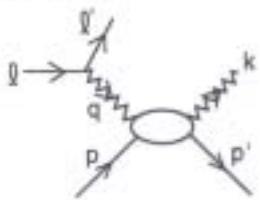
HHC maintained

$$\frac{F_2(Q^2)}{F_1(Q^2)} = \frac{M_A}{1 + \frac{Q^2}{96 \text{ GeV}^2} \log^{-0.6} \left(\frac{(1+Q^2)/4 M_A^2}{\mu_F^2} \right)}$$



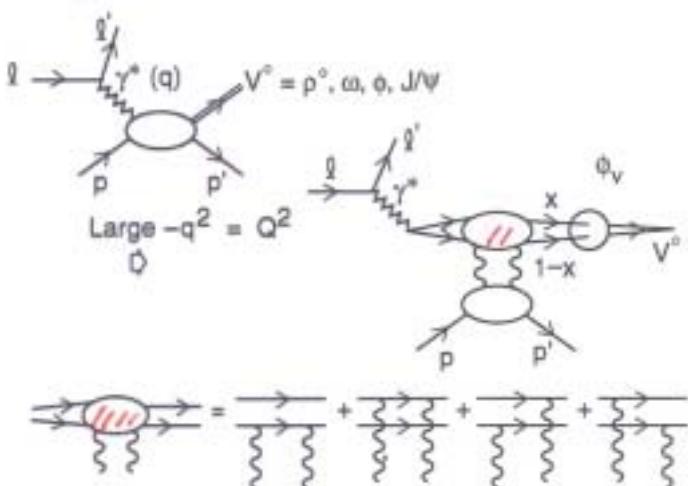
(f) Virtual Compton $\gamma^* p \rightarrow \gamma' p'$
 $\langle p' \lambda' | J^\mu(z) J^\nu(0) | p \lambda \rangle$

$$\text{Large } -q^2 = Q^2$$



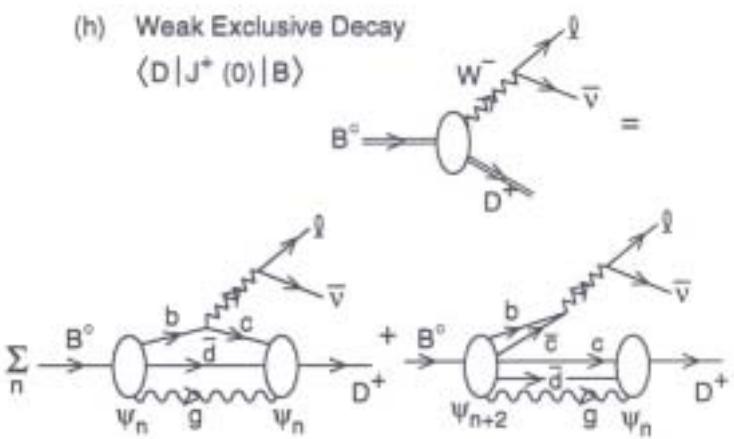
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(g) Vector Meson Leptoproduction $\gamma^* p \rightarrow V^* p'$



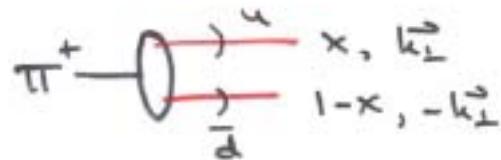
(h) Weak Exclusive Decay

$\langle D | J^+(0) | B \rangle$



Pion Distribution Amplitude

$$\phi_\pi(x, Q^2) = \int \frac{d^2 k_\perp}{16\pi^2} \Psi_{q\bar{q}/\pi}^{(0)}(x, \vec{k}_\perp)$$



$$\sim \Psi_{q\bar{q}/\pi}(x, b_\perp \sim O(\frac{1}{Q}))$$

$$\begin{aligned} \phi_\pi(x, Q) &= \int \frac{dz^- p_\pi^+}{4\pi} e^{i x p_\pi^+ z^- / 2} \\ &\quad \left. \langle 0 | \bar{\psi}^{(0)} \frac{\gamma^+ \gamma^5}{2\sqrt{2} n_c} \psi(z) | \pi \rangle \right|_{z^+ = \vec{z}_\perp = 0}^{(Q)} \end{aligned}$$

$$P_{exp} \int_0^1 ds i g_A(sz) \cdot z = 1 \quad \text{in } A^+ = 0$$

from

$$= \int \frac{dk^-}{2\pi} \Psi_{BS}(k, p)$$

Obey: OPE, RGE, Evolution Eq.